Test 3 - Calculus II (Spring 2015)

INSTRUCTIONS: Complete each of the following problems in your Bluebook. Each problem is worth a maximum of 12 points. Points will be awarded for both completeness and clarity of solutions. Partial credit will be awarded for partial solutions. Please recall that cell phones and graphing calculators are not allowed on this exam.

1. Determine the convergence or divergence of the following series. Clearly justify your answer.

(a)
$$\sum_{k=1}^{\infty} \left(\frac{2k^2}{5k^2+k}\right)^k$$
 (b) $\sum_{k=1}^{\infty} (-1)^k \cdot \frac{k}{2k+15}$

2. Determine whether the series $\sum_{n=0}^{\infty} (-1)^n \left(\frac{n}{n^{3/2} + 10}\right)$ converges absolutely, converges conditionally, or diverges. Clearly justify your answer.

3. Find the fourth degree term of the Maclaurin series expansion for $(x + 1)^{5/2}$.

4. Determine the interval of convergence of the power series $\sum_{n=1}^{\infty} \frac{(x-3)^n}{2^n \sqrt{n}}.$

5. Find the Maclaurin series expansion for xe^{5x} , and determine its interval of convergence.

BONUS. (+12 points) Compute the values of the following convergent infinite series. Credit will only be awarded for clearly justified answers.

(a)
$$\sum_{k=1}^{\infty} \frac{(-1)^{k+1}}{k} = 1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \frac{1}{5} - \frac{1}{6} + \dots$$

(b)
$$\sum_{k=0}^{\infty} \frac{4 \cdot (-1)^k}{2k+1} = 4 - \frac{4}{3} + \frac{4}{5} - \frac{4}{7} + \frac{4}{9} - \frac{4}{11} + \dots$$

(c)
$$\sum_{k=0}^{\infty} \frac{1}{k!} = 1 + \frac{1}{1!} + \frac{1}{2!} + \frac{1}{3!} + \frac{1}{4!} + \frac{1}{5!} + \frac{1}{6!} + \dots$$

(d)
$$\sum_{k=0}^{\infty} \frac{(-1)^k}{k!} = 1 - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!} + \frac{1}{4!} - \frac{1}{5!} + \frac{1}{6!} + \dots$$